An Abstract Class Loader for the SSP and its Implementation in TL

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Abstract

The SSP is a hardware implementation of a subset of the JVM for use in high consequence embedded applications. In this context, a majority of the activities belonging to class loading, as it is defined in the specification of the JVM, can be performed statically. Static class loading has the net result of dramatically simplifying the design of the SSP as well as increasing its performance. Due to the high consequence nature of its applications, strong evidence must be provided that all aspects of the SSP have been implemented correctly. This includes the class loader. This article explores the possibility of formally verifying a class loader for the SSP implemented in the strategic programming language TL. Specifically, an implementation of the core activities of an abstract class loader is presented and its verification in ACL2 is considered.
Contents

1 Introduction ........................................ 7
  1.1 The ROM Images Executed by the SSP ................. 7
  1.2 An Overview of Class Loader Requirements .............. 9

2 Overview of the Structure of Class Files .............. 12
  2.1 Index Resolution ................................ 12
  2.2 Static Field Address Calculation ..................... 14
  2.3 Instance Field Offset Calculation .................... 15
  2.4 Method Table Construction ........................ 15
  2.5 Inter-class Absolute Address and Offset Address Distribution . 17

3 An overview of TL .................................. 18
  3.1 The Basic Constructs of TL ......................... 19
  3.2 Tree/Term Notation ................................ 20
  3.3 Conditional Rewrite Rules .......................... 21
    3.3.1 Conditions .................................. 21
    3.3.2 Rule Application ............................. 22
  3.4 Combinators ...................................... 22
  3.5 Generic First-Order Traversals ...................... 23
  3.6 Higher-Order Rules and Strategies .................. 23
  3.7 Higher-Order Generic Traversals .................... 23

4 A Strategic Implementation of the Class Loader Core ... 24
  4.1 Index Resolution in TL ............................ 28
  4.2 Static Field Address Calculation in TL .............. 29
  4.3 Instance Field Offset Calculation in TL ............. 30
  4.4 Method Table Construction in TL .................... 32
  4.5 Inter-class Absolute Address and Offset Address Distribution in TL . 34

5 Verification and Validation .......................... 35
  5.1 The ACL2 Theorem Prover .......................... 35
  5.2 Modelling TL in ACL2 .............................. 36
  5.3 Verification of the Correctness of the Transformation Rules .... 37

6 Related Work ....................................... 41
  6.1 Rewriting and Strategic Programming .................. 41
  6.2 Verification ...................................... 42

7 Conclusion ......................................... 42
List of Figures

1 Resolution of indexes (aka. encoded symbolic references) ........................................... 9
2 The components of a Java class file .................................................................................... 13
3 The subset of the Java class file structure relevant to the class loader core ....................... 13
4 A constant pool description of the integer field B.x ......................................................... 14
5 Classes and their static fields .............................................................................................. 15
6 Mapping static fields to absolute heap addresses ............................................................... 15
7 Classes and their instance fields ......................................................................................... 16
8 Mapping instance fields to object offsets ......................................................................... 16
9 Mapping instance fields to object offsets ......................................................................... 16
10 Classes and their virtual methods ...................................................................................... 17
11 Method table construction ................................................................................................. 17
12 An examples of two classes having external symbolic references to fields and methods ... 18
13 Inter-class distribution of field offset/address and method table offsets ......................... 18
14 A concrete syntax fragment ............................................................................................... 21
15 The syntactic structure of rewrite rules in TL ................................................................. 21
16 An extended-BNF grammar describing a simplified application in terms of a list of class files ................................................................. 25
17 Three abstract class files prior to class loading ............................................................... 26
18 The three abstract class files shown in Figure 17 after class loading ............................... 27
19 Index Resolution ................................................................................................................ 28
20 A TL strategy for absolution address calculation ............................................................ 30
21 Offset address calculation .................................................................................................. 31
22 Method table construction ................................................................................................. 33
23 Inter-class distribution ....................................................................................................... 35

Nomenclature

BNF    Backus-Naur Form
HATS   High Assurance Transformation System
IDE    Integrated Development Environment
JVM    Java Virtual Machine
ROM    Read Only Memory
SSP    Sandia Secure Processor
TL     Transformation Language – a higher-order strategic programming language
1 Introduction

At Sandia National Laboratories, a subset of the Java Virtual Machine (JVM) has been developed in hardware for use in high-consequence embedded applications. The implementation is called the Sandia Secure Processor (SSP) [11][24] and supports a subset of Java bytecodes as its native instruction set.

This paper has three objectives: (1) to informally describe the core functionality of the class loader for the SSP, (2) to demonstrate how the abstract functionality of this core class loader can be implemented using higher-order strategic programming techniques, and (3) to discuss how the correctness of the class loader can formally verified. The paper is organized as follows. We begin with an introduction to the goals of the SSP class loader. Section 2 gives an overview of the Java class file structure and restricts our attention to the subset of class files impacted by the SSP class loader core. This section also gives an informal description of the core activities of the SSP class loader. Section 3 gives an overview of the higher-order strategic programming language TL. Section 4 presents and discusses a TL implementation of an abstract class loader core. Section 5 describes preliminary efforts at verifying and validating the transformations.

1.1 The ROM Images Executed by the SSP

An application program for the SSP is called a ROM image and consists of a collection of class file images stored on a Read-Only Memory (ROM). The image of a class file in the ROM contains (1) a ROM constant pool and (2) a method table and methods section. For the purposes of this article, there are two major differences between ROM constant pools and the constant pools found in Java class files. The first major difference is that in ROM constant pools, class, field, and method entries are represented in terms of absolute addresses or offset addresses together with additional data that, broadly speaking, provides type information describing the entry. In contrast, in Java class files such entries are represented as encodings of symbolic references. In this article, we refer to the aggregation of one or more constant pool indexes as an encoding of a symbolic reference. The second major difference is that, unlike the constant pools in Java class files, ROM constant pools do not contain any name_and_type, name, and Utf8 entries. Thus constant pools in the ROM are limited to the following entries: constant integer, constant long, static field, instance field, class, and method. Among the method entries, in this article, we restrict our consideration only to virtual methods. That is, methods that are invoked within an application program using the invokevirtual bytecode. In this article, we do not consider static or special methods whose invocations are respectively achieved through the invokevirtual and invokespecial bytecodes. This restriction to virtual methods is essentially without loss of generality. The one exception being an anomalous case involving dynamic binding of a method that has been invoked using the invokespecial bytecode [10][19].

In a ROM image, the methods section of class files have also been modified. In particular, within the bytecode of a method, constant pool indexes (i.e., encodings of symbolic references) have been replaced with offset addresses into the ROM constant pool. These are the major differences between class files as produced by a Java compiler and as they appear on the ROM.

Due to the similarity between the JVM and the SSP, the primary goal of the class loader for the SSP can be simply stated:
The Primary Goal of the SSP Class Loader:

*Resolve* encoded symbolic references (indexes) in class files to absolute addresses or offset addresses.

Though the focus on this paper is on the primary goal as stated above, we would like to mention that there are numerous secondary goals a class loader for the SSP must satisfy. These secondary goals include the construction of various kinds of type data associated with constant pool entries, padding method bodies so methods begin and end on word boundaries, and so on.

Within the SSP, absolute addresses belong to one of two domains. These domains model the address spaces of the ROM and heap respectively. The first domain, $D_{ROM}$, describes the location of bytes within the ROM image. Addresses belonging to $D_{ROM}$ are used to describe the location of immutable structures associated with a class such as the location of a ROM constant pool, the starting address of a method, and the method table associated with a class. The second domain, $D_{HEAP}$, describes the location of bytes within the SSP’s heap memory. From the perspective of the class loader, absolute addresses belonging to $D_{HEAP}$ are used solely to describe the location of static fields. All other assignments of absolute addresses in $D_{HEAP}$ occur during runtime. For example, during execution bytecodes such as `new` are responsible for heap memory allocation. These allocations yield absolute addresses in $D_{HEAP}$ belonging to objects (i.e., object references).

In contrast to absolute addresses, offset addresses are used to describe the location of data in a relative fashion. Adding an offset address to an appropriate absolute address (such as the start of a constant pool) yields an absolute address that describes the location of a particular data item within an absolute address space (e.g., the address of a constant pool entry). The design of the SSP makes use of three types of offset addresses: constant pool offsets, method table offsets, and object offsets. Constant pool offset addresses are values belonging to the domain $D_{CP}$ and describe offsets relative to the start of a ROM constant pool. Semantically speaking, constant pool offset addresses are used to describe the location of ROM constant pool entries. Method table offset addresses are values belonging to the domain $D_{MT}$ and describe offsets relative to the start of a method table residing in the ROM. Semantically speaking, method table offset addresses are used to describe the location of entries in a method table. Method table entries contain information needed to execute a particular virtual method. This information includes the starting address of the virtual method, the absolute address of the constant pool associated with this virtual method, and type information defining the number of local variables and parameters used by the method. And lastly, object offset addresses are values belonging to $D_{OBJ}$ and describe offsets relative to the start of an object (i.e., an instance of a class). Semantically speaking, object offset addresses are used to describe the location of data within an object. This data consists primarily of the object’s instance fields. However, the first data entry of an object is an absolute address belonging to $D_{ROM}$ describing the location of the class from which this object is an instance (this is needed when a method for this object is invoked).
<table>
<thead>
<tr>
<th>Context where Index Occurs</th>
<th>Interpretation of Resolution</th>
</tr>
</thead>
<tbody>
<tr>
<td>within a bytecode in the body of a method</td>
<td>ROM constant pool offset address where the type of the constant pool entry can be inferred from the bytecode</td>
</tr>
<tr>
<td>this_class</td>
<td>absolute address in ROM</td>
</tr>
<tr>
<td>super_class</td>
<td>absolute address in ROM</td>
</tr>
<tr>
<td>class entry in ROM constant pool</td>
<td>absolute address in ROM</td>
</tr>
<tr>
<td>static field entry in ROM constant pool</td>
<td>absolute address in heap</td>
</tr>
<tr>
<td>static field entry in fields section of class file</td>
<td>absolute address in heap</td>
</tr>
<tr>
<td>instance field entry in ROM constant pool</td>
<td>object offset address</td>
</tr>
<tr>
<td>instance field entry in fields section of class file</td>
<td>object offset address</td>
</tr>
<tr>
<td>virtual method entry in ROM constant pool</td>
<td>ROM method table offset address</td>
</tr>
<tr>
<td>virtual method entry in ROM method table</td>
<td>absolute address of method in ROM</td>
</tr>
</tbody>
</table>

Figure 1: Resolution of indexes (aka. encoded symbolic references)

Given an index, the type of address to which it should be resolved can be uniquely determined from the context in which it is used. Figure 1 lists the contexts that must be considered.

1.2 An Overview of Class Loader Requirements

Within an application program, classes may be ordered to form inheritance hierarchies through the Java “extends” directive. The subtype relation resulting from inheritance hierarchies impose constraints on how object offsets and method table offsets must be calculated. These constraints as well as others can be expressed in the form of properties that a resolved collection of encoded symbolic references must possess in order to be correct. A non-exhaustive list of these properties follows.

- **Unique-Offset**: Within the scope of an inheritance hierarchy, all instance fields must be resolved to unique object offsets. *Rationale*: This property ensures that two instance fields are not mapped to the same offset.

- **Consistent-Offset**: Instance fields must be resolved to offsets in a manner that is consistent with upcasting. *Rationale*: This property ensures that the mapping of instance fields to offsets is treated in a consistent fashion for all classes belonging to an inheritance hierarchy.

- **Non-Overlapping-Addresses**: The values of primitive types supported by the SSP must be mapped to memory regions that are sufficiently large to hold all legal values of that type. For example, an integer field must be mapped to a memory region that is at least 32-bits wide. *Rationale*: This property prevents instance fields from being packed so tightly within an object that their memory spaces overlap. This property also prevents static fields from being packed so tightly in the heap that their memory spaces overlap. Note that simply requiring that instance fields have unique offsets is not sufficient to ensure this property.
• **Unique-Address**: Within an application, all static fields must be resolved to a unique absolute address within the heap. *Rationale*: This requirement ensures that two static fields are not mapped to the same absolute address within the heap.

• **Consistent-Method-Invocation**: Virtual method invocations must be referred to indirectly via an offset to a method table. Furthermore, within an inheritance hierarchy all method tables must be consistent with respect to the positioning of method table entries. *Rationale*: Positional table entry consistency among method tables within an inheritance hierarchy ensures that proper method invocation will result in the presence of upcasting.

• **Address Units**
  
  - Constant pool offset addresses must be in word units (i.e., 32-bit quantities) in the range $0 \leq cp_{-}offset < 2^{16}$. The only range exception being that of the ldc bytecode which has the range $0 \leq cp_{-}offset < 2^{8}$. *Rationale*: This requirement ensures that spacial requirements of constant pool indexes in bytecodes match the spatial requirements of offset addresses into a ROM constant pool. This requirement also guarantees that the addressing scheme of the SSP will be able to handle all Java constant pools having $2^{15}$ elements or less, with $2^{15}$ being a conservative (guaranteed achievable) lower bound. The class loader must flag as an error all constant pools whose element count exceed this threshold.
  
  - Method table offsets must be in word units in the range $0 \leq mt_{-}offset < 2^{16}$. *Rationale*: This design decision enables the addressing scheme of the SSP to handle Java classes whose total number of virtual methods (both declared and inherited) is less than or equal to $2^{16}$. The class loader must flag as an error all classes whose virtual method count exceeds this threshold.
  
  - Absolute addresses in the heap must be in byte units in the range $0 \leq address < 2^{24}$. *Rationale*: This enables a Java constant pool entry containing a symbolic reference to a static field to be resolved to a one-word ROM constant pool entry describing the type (8-bits) and absolute heap address (24-bits) of the static field.

  The list given above is not meant to be complete, but rather to give the reader a feeling for the necessary kinds of properties that must be satisfied in order for the resolution performed by a class loader to be considered correct. Taking a more rigorous approach, correctness properties of the kind just described can be formalized and expressed in terms of a formula $\mathcal{C}$ in first-order logic. Abstractly speaking, this formula defines properties and relationships between (1) encoded symbolic references and addresses, and (2) addresses within an address space.

  In addition to correctness properties, the resolution of encoded symbolic references must also satisfy a number of efficiency-based constraints. A number of these constraints are related to optimization of memory usage and access. However, fault-tolerance, safety, and security constraints are also possible. A non-exhaustive list of these constraints follows.

  • **Spatial-Efficiency**:
– Instance fields should be packed as tightly as possible in objects and static fields should be tightly packed in the heap. *Rationale:* This is a necessary condition to assure that heap memory is efficiently utilized.

– Object offset addresses must be in byte units (i.e., 8-bit quantities). *Rationale:* This design decision enables sequences of short, char, byte, and boolean fields to be closely packed within an object.

• **Temporal-Efficiency:**

  – 64-bit values (i.e., longs) should not span 32-bit boundaries within the heap or ROM address space. For example, a long may be stored at byte address 0x0000 or 0x0004 but should not be stored at byte address 0x0002 because retrieving a long value stored in this manner would require 3 memory fetches instead of 2. *Rationale:* This is a necessary condition to assure that the SSP executes efficiently.

  – 32-bit values such as integers and references should not span 32-bit boundaries within the heap or ROM address space. For example, an integer value may be stored at byte address 0x0000 or 0x0004 but should not be stored at byte address 0x0002 because retrieving a value stored in this manner would require 2 memory fetches instead of 1. *Rationale:* This is a necessary condition to assure that the SSP executes efficiently.

  – 16-bit values such as shorts and chars should not span 16-bit boundaries within the heap or ROM address space. *Rationale:* This is a necessary condition to assure that the SSP executes efficiently.

This list of hardware constraints is not meant to be exhaustive, but rather it demonstrates the nature of the constraints imposed by the SSP hardware. Taking a more rigorous approach, hardware constraints can be expressed in terms of a formula $\mathcal{H}$ in first-order logic. Abstractly speaking, this formula defines properties and relationships between (1) encoded symbolic references and addresses, and (2) addresses within an address space.

Given the formula $\mathcal{C} \land \mathcal{H}$ an interpretation $I$ is a mapping from encoded symbolic references in $\mathcal{C}$ to the domain $D_{\text{def}} = D_{\text{HEAP}} \cup D_{\text{ROM}} \cup D_{\text{CP}} \cup D_{\text{MT}} \cup D_{\text{OBJ}}$ of absolute addresses and offset addresses. In this setting, resolution for the SSP can be defined as a function that constructs an interpretation $I$ over $D$ satisfying the formula $\mathcal{C} \land \mathcal{H}$. From an operational perspective, the interpretation $I$ is an assignment of address values to indexes (i.e., encoded symbolic references). In this article, the terms *resolution* and *resolve* are used to describe the processes behind the construction of such assignments.

We are now in a position to give a high-level definition of the class loader core that is the focus of this article.

**Definition 1** The **core of the class loader for the SSP** is an interpretation $I_{\text{core}}$ mapping indexes to (1) offset addresses in $D_{\text{MT}} \cup D_{\text{OBJ}}$, and (2) absolute addresses in the space $D_{\text{HEAP}}$ such that $I_{\text{core}}$ satisfies $\mathcal{C} \land \mathcal{H}$.
Notice that the definition of the core, as we have defined it, excludes the offset address space $D_{CP}$ and the absolute address space $D_{ROM}$. The reason for excluding these address spaces from consideration by the core is mainly for simplicity and space considerations. For example, calculating offsets for the constant pool entries is essentially the same as calculating offsets for method table entries. Since method table construction is included in the core the notion of calculating offsets for tables is already covered in the core. The calculation of absolute addresses for immutable objects in the ROM is also abstractly similar to table offset calculation and is also therefore omitted.

2 Overview of the Structure of Class Files

Figure 2 gives a top-level view of the components contained in a Java class file. Components such as cp_info, interfaces, field_info, and method_info are highly complex and contain a number of subcomponents which are not shown in Figure 2. For more information about the structure of these components as well as class files in general see [10][19].

In this paper we restrict our attention to class loading activities for the SSP pertaining to the subset of Java class files shown in Figure 3. In particular, we will look at (1) index resolution, (2) static field address calculation, (3) offset address calculation, (4) method table construction, and (5) inter-class absolute address and offset address distribution. Collectively, we will refer to this set of class loading activities as the class loader core. In the following sections we informally describe each of these activities in detail.

2.1 Index Resolution

In Java class files, references to field, method, this-class, and super-class information are abstractly encoded as indexes into the class file’s constant pool. Within a constant pool, such indexes directly or indirectly denote information that is ultimately expressed symbolically in terms of Utf8 strings. We will refer to the symbolic information denoted by an index as the abstract meaning otherwise known as the symbolic reference of that index. We use the term index resolution to denote the process of constructing the abstract meaning of indexes.

Consider the constant pool fragment shown in Figure 4. In this example, much detail has been abstracted away from the structure of the constant pool, and only the salient portions remain. For example, Java constant pool entries have tags that indicate the type of the entry, and Utf8 entries are realized in terms of a list of bytes. However, regardless of the presence or absence of such detail the concept of index resolution remains the same.

Given the abstracted constant pool in the Figure 4, we ask “What is the symbolic reference of the index 1 with respect to this constant pool”? To determine the meaning of an index, the chain of index/value pairs are followed until a collection of Utf8 values are reached. The concatenation of these Utf8 values forms the symbolic reference. The value at index 1 in the constant pool contains an entry of type CONSTANT_Fieldref_info, which indicates that the index 1 denotes an encoding of a symbolic reference to a field. When resolved this symbolic reference will consist of the name of the class in which the field is declared, the name of the field, and a descriptor describing the type of the field (e.g., integer, short, long). The contents of the CONSTANT_Fieldref_info entry at position 1 consists of two indexes.
magic

The hex value 0xCAFE BABE indicating that this file
is a Java class file.

minor_version

The minor version of the compiler that produced this class.

major_version

The major version of the compiler that produced this class.

constant_pool_count

The number of entries in the constant pool.

cp_info

The constant pool.

access_flags

Modifiers associated with this class or interface
(e.g., private, final, abstract, etc.).

this_class

A constant pool index that when resolved yields the
name of the class.

super_class

The value 0 or a constant pool index that when resolved
yields the name of the super class.

interfaces_count

The number of direct super interfaces of the class or interface.

interfaces

The interfaces implemented by the class.

fields_count

The number of fields explicitly declared in the class.

field_info

The fields explicitly declared in the class.

methods_count

The number of methods explicitly declared in the class.

method_info

The methods explicitly declared in the class.

attributes_count

The number of attributes of the class.

attribute_info

The attributes of the class.

Figure 2: The components of a Java class file

<table>
<thead>
<tr>
<th>Java Structure Name</th>
<th>SSP Structure Name</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>cp_info</td>
<td>cp</td>
<td>the constant pool</td>
</tr>
<tr>
<td>this_class</td>
<td>this</td>
<td>the name of this class</td>
</tr>
<tr>
<td>super_class</td>
<td>super</td>
<td>the name of the parent class</td>
</tr>
<tr>
<td>field_info</td>
<td>sfields &amp; ifields</td>
<td>fields are separated into a list of static fields sfields and a list of instance fields ifields</td>
</tr>
<tr>
<td>method_info</td>
<td>mt &amp; methods</td>
<td>methods are associated with a method table mt</td>
</tr>
</tbody>
</table>

Figure 3: The subset of the Java class file structure relevant to the class loader core
The Java class file specification requires that the first index be interpreted as a class index denoting the class in which the field is declared. The second index should be interpreted as a name and type index which provides information about the name and type of the field. Thus the first step in the index resolution process is: 1 ⇒ 2 3. Next, index resolution is individually performed on the indexes 2 and 3. The constant pool entry having index 2 contains a name index 4. Thus, the current state of the resolution is: 1 ⇒ 2 3 ⇒ 4 3. Now, the constant pool entry having index 4 contains an entry of type CONSTANTUtf8 whose value is “B”. Thus, “B” is the name of the class in which the field denoted by index 1 is declared.

The second part of the value located at index 1 in the constant pool is the index 3. The constant pool entry at index 3 contains a name index 5 that in this context denotes the name of the field, and a descriptor index 6 denoting the type of the field. Thus, 3 ⇒ 5 6. The contents of the constant pool at index 5 tells us that the name of the field is the Utf8 value “y”. The contents at index 6 indicates that the field is of type “I”. Thus, the symbolic reference of index 1 with respect to the given constant pool is B y I, that is, index 1 denotes the field y of type integer that is declared in class B. The index resolution of 1 can be summarized by the following rewrite sequence:

\[ 1 \Rightarrow 2 \ 3 \Rightarrow 4 \ 3 \Rightarrow B \ 3 \Rightarrow B \ 5 \ 6 \Rightarrow B \ y \ 6 \Rightarrow B \ y \ I \]

In general, index resolution concerns itself with the replacement of indexes with their symbolic references. The scope of this type of rewriting is limited to individual class files and is based solely on information found in the constant pool for the class. Complete details on the structure of constant pools can be found in the literature [10][19].

### 2.2 Static Field Address Calculation

The goal of static field address calculation is to assign a unique absolute address to each static field within a Java application. Since static fields are associated with a class rather than an object (i.e., an instance of a class), their number remains constant during runtime. Consider the Java application program shown in Figure 5 consisting of the classes B, C, and D.

If we assume a byte-addressable memory in the range 0x0000...0xFFFF, then the static fields in the application could be assigned to the absolute addresses as shown in Figure 6. From a semantic perspective this class loader activity can be seen as providing an interpretation (i.e., a concrete meaning) for the symbolic references of static fields.
2.3 Instance Field Offset Calculation

Instance fields, in contrast to static fields, are associated with objects rather than classes. Each object contains its own copy of every instance field declared in its corresponding class plus all of the instance fields inherited from its super class. Figure 7 shows the instance field declarations in a number of Java class fragments.

Figures 8 and 9 show possible offset calculations respectively for the instance fields of class C and E. We would like to point out that the class loader does not actually construct objects of the kind shown in Figures 8 and 9. That functionality is entrusted to the microcode implementation of the bytecode new. Instead, the purpose of the class loader is to construct an interpretation (i.e., assign a concrete semantics) in the form of a mapping from symbolic references of instance fields to object offset addresses in a manner that is consistent with the formula CH mentioned in Section 1.2. The interpretation provided by the object offset addresses must be sound with respect to all dynamic uses of objects. For example, in Java objects can be dynamically upcast and downcast. Thus all objects within an inheritance hierarchy must have a consistent interpretation for all shared (i.e., inherited) instance fields.

2.4 Method Table Construction

Encoded symbolic references to methods must ultimately be resolvable to the address where the bytecode for the method resides. However, this resolution is complicated by the interplay of two aspects of Java’s subtype system. First, within an inheritance hierarchy multiple definitions for a single method may occur. Second, Java’s upcast operation provides a mechanism by which the type of an object may be cast to that of any ancestor belonging to the inheritance chain.

Within such a fluid inheritance hierarchy, methods must utilize symbolic method references in a consistent fashion. Consistency here means that a symbolic reference to a method such as B.foo must
have the ability to denote any redefinition of \texttt{foo} in every descendent of \texttt{B}. This capability is needed because during runtime, an object that is an instance of a descendent of \texttt{B} may be upcast to \texttt{B} after which the method \texttt{foo} could be invoked on the upcast object. In such a case, the constant pool of the class in which \texttt{B.foo} is invoked will contain a symbolic reference to \texttt{B.foo}. However, because multiple definitions of \texttt{foo} may exist throughout the inheritance hierarchy this symbolic reference cannot be directly resolved to a single absolute address. A standard solution to this problem is to construct a method table for each class \cite{10}[19]. This method table forms a layer of indirection that enables methods to be referenced in a consistent fashion. The entries in a method table contain data necessary to execute the bytecode corresponding to the implementation of a method as seen from the perspective of a particular class. For example, data in a method table may include the address of the first bytecode in the method as well as the address the method’s corresponding constant pool. Symbolic references to methods such as \texttt{B.foo} are now resolved to offsets into the method table. Of course in order for the indirection provided by the method table solve our problem, all classes that inherit or redefine \texttt{foo} must
store data related to foo in the same relative position (i.e., offset) in their method table.

Figure 10 shows a class B and a class C which extends B. Note that although the method foo is redeclared in C, the method tables for B and C, shown in Figure 11, place the data for foo in the same relative location in their method tables. As a result, the symbolic reference to B.foo can be uniformly resolved to the method table offset 0x0008. Which method table this offset is applied to depends on the class from which an object is derived (e.g., B or C in Figure 10). For example, the expression 
((B)(new C())).foo() will access the data at offset 0x0008 in C’s method table while the expression (new B()).foo() will access the data at offset 0x0008 in B’s method table.

class B
{
    ...  
    int f1(int x) {...}
    int foo() {...}
    int g1() {...}
    ...
}

class C extends B { ...
    int foo() {...}
    int g2() {...}
    ...
}

Figure 10: Classes and their virtual methods

<table>
<thead>
<tr>
<th>Offset</th>
<th>Method Table for B</th>
<th>Comment</th>
</tr>
</thead>
<tbody>
<tr>
<td>0x0000</td>
<td>data for B.f1(I)I</td>
<td>declared</td>
</tr>
<tr>
<td>0x0008</td>
<td>data for B.foo()I</td>
<td>declared</td>
</tr>
<tr>
<td>0x0010</td>
<td>data for B.g1()I</td>
<td>declared</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Offset</th>
<th>Method Table for C</th>
<th>Comments</th>
</tr>
</thead>
<tbody>
<tr>
<td>0x0000</td>
<td>data for B.f1(I)I</td>
<td>inherited</td>
</tr>
<tr>
<td>0x0008</td>
<td>data for C.foo()I</td>
<td>redeclared</td>
</tr>
<tr>
<td>0x0010</td>
<td>data for B.g1()I</td>
<td>inherited</td>
</tr>
<tr>
<td>0x0018</td>
<td>data for C.g2()I</td>
<td>declared</td>
</tr>
</tbody>
</table>

Figure 11: Method table construction

2.5 Inter-class Absolute Address and Offset Address Distribution

Inter-class distribution is concerned with the distribution of absolute addresses and offset addresses between the various class files that make up a Java application. Within a single class file, symbolic references to locally declared fields and methods can be resolved to absolute addresses (for static fields), object offsets (for instance fields), and method table offsets (for methods). However, within a Java application, a class file X may have a symbolic reference to fields and methods that have been declared in another class file Y. References external to X show up as symbolic references in the constant pool of X and must be resolved using information originating from the class Y. Specifically, absolute address and offset address information must be distributed from the class in which the declarations occur (e.g., Y) to all classes referencing these declarations (e.g., X).

17
Figure 12 shows two class files B and C. The constant pool of class file B contains symbolic (non-local) references to a field and method declared in (local to) C, and the constant pool of C contains symbolic references to a field and method declared in B.

<table>
<thead>
<tr>
<th>Class B</th>
<th>Index</th>
<th>Constant Pool Entries</th>
<th>Fields</th>
<th>Method Table Offset</th>
<th>Method Table Info</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>B.x I local</td>
<td></td>
<td>B.w I 0x0000</td>
<td>0x00</td>
<td>B.g (I)I ...</td>
</tr>
<tr>
<td>2</td>
<td>C.x I non-local</td>
<td></td>
<td>B.x I 0x0004</td>
<td>0x01</td>
<td>B.f (I)I ...</td>
</tr>
<tr>
<td>3</td>
<td>B.f (I) local</td>
<td></td>
<td>B.y I 0x0008</td>
<td>0x02</td>
<td>B.foo (I)I ...</td>
</tr>
<tr>
<td>4</td>
<td>C.g (I) non-local</td>
<td></td>
<td>–</td>
<td>–</td>
<td>–</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Class C</th>
<th>Index</th>
<th>Constant Pool Entries</th>
<th>Fields</th>
<th>Method Table Offset</th>
<th>Method Table Info</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>B.x I non-local</td>
<td></td>
<td>C.x I 0x0000</td>
<td>0x00</td>
<td>C.bar (I)I ...</td>
</tr>
<tr>
<td>2</td>
<td>C.x I local</td>
<td></td>
<td>C.y I 0x0004</td>
<td>0x01</td>
<td>C.f (I)I ...</td>
</tr>
<tr>
<td>3</td>
<td>B.f (I) non-local</td>
<td></td>
<td>C.z I 0x0008</td>
<td>0x02</td>
<td>C.g (I)I ...</td>
</tr>
<tr>
<td>4</td>
<td>C.g (I) local</td>
<td></td>
<td>C.k I 0x000C</td>
<td>0x03</td>
<td>C.h (I)I ...</td>
</tr>
</tbody>
</table>

Figure 13 shows the class files B and C after the inter-class distribution phase. Note that field address and method table offset data has been propagated between the classes.

<table>
<thead>
<tr>
<th>Class B</th>
<th>Index</th>
<th>Constant Pool Entries</th>
<th>Fields</th>
<th>Method Table Offset</th>
<th>Method Table Info</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>B.x I 0x0004</td>
<td></td>
<td>B.w I 0x0000</td>
<td>0x00</td>
<td>B.g (I)I ...</td>
</tr>
<tr>
<td>2</td>
<td>C.x I 0x0000</td>
<td></td>
<td>B.x I 0x0004</td>
<td>0x01</td>
<td>B.f (I)I ...</td>
</tr>
<tr>
<td>3</td>
<td>B.f (I) 0x01</td>
<td></td>
<td>B.y I 0x0008</td>
<td>0x02</td>
<td>B.foo (I)I ...</td>
</tr>
<tr>
<td>4</td>
<td>C.g (I) 0x02</td>
<td></td>
<td>–</td>
<td>–</td>
<td>–</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Class C</th>
<th>Index</th>
<th>Constant Pool Entries</th>
<th>Fields</th>
<th>Method Table Offset</th>
<th>Method Table Info</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>B.x I 0x0004</td>
<td></td>
<td>C.x I 0x0000</td>
<td>0x00</td>
<td>C.bar (I)I ...</td>
</tr>
<tr>
<td>2</td>
<td>C.x I 0x0004</td>
<td></td>
<td>C.y I 0x0004</td>
<td>0x01</td>
<td>C.f (I)I ...</td>
</tr>
<tr>
<td>3</td>
<td>B.f (I) 0x01</td>
<td></td>
<td>C.z I 0x0008</td>
<td>0x02</td>
<td>C.g (I)I ...</td>
</tr>
<tr>
<td>4</td>
<td>C.g (I) 0x02</td>
<td></td>
<td>C.k I 0x000C</td>
<td>0x03</td>
<td>C.h (I)I ...</td>
</tr>
</tbody>
</table>

Figure 13: An overview of TL

The specification of the JVM enables class loading to occur dynamically (e.g., during runtime). However, from the perspective of class loading, the SSP can be considered a closed system because all the class files in an application must be stored on the ROM prior to execution. The closed nature of the SSP’s
execution environment enables the class loading activities of the SSP to be performed statically, prior to execution. Under these conditions, the functionality of a class loader is well suited to a transformation-oriented implementation [25]. This section gives an overview of the strategic programming language TL which we will use to implement an abstract version of the class loader core.

In general, strategic programming systems are rewriting systems that have been extended with a variety of constructs enabling explicit control over the application of rewrite rules. Such control is typically necessary when dealing with rule sets that are non-confluent and/or non-terminating. When constructed appropriately, rewriting systems and strategic programming systems have properties that make them well-suited to formal verification. Our research goal into the development of TL has been to provide a framework whereby strategic programs can be written to realize complex functionality in a manner which nevertheless remains within the grasp of formal automated verification.

3.1 The Basic Constructs of TL

TL is a higher-order strategic programming language [26][29][27][28]. In TL, conditional rewrite rules can be combined to form expressions called strategies. Strategies define controlled sequences of rewrites and can be applied to tree structures to produce other tree structures. Thus, a strategy can be viewed as a function that rewrites or transforms one tree into another.

The primary constructs and abstractions in a first-order strategic programming language typically include:

1. patterns – A pattern is a notation for describing the tree structures that are being manipulated. This notation typically includes variables, potentially typed, that are quantified over a variety of tree structures.

2. rewrite rules – A rewrite rule is a construct for specifying that one pattern is to be replaced by another pattern. In a strategic system, rewrite rules are also considered to be a degenerative form of strategy.

3. conditions – A condition is a construct associated with a rewrite rule that restricts its application.

4. combinators – A combinator is an operator (generally unary or binary) that can be used to compose one or more strategies into a new strategy.

5. generic traversals – A generic traversal can be thought of as a curried function parameterized on a strategy s and a tree t. As the name suggests, a generic traversal will traverse its input tree structure t and apply its input strategy s at one or more points along the traversal. A typical and very useful generic traversal is one that performs a top-down left-to-right traversal of a tree structure and uniformly applies its input strategy to all sub-trees encountered.

6. strategies – In its purest sense, a first-order strategy can be characterized as any function that transforms one tree into another tree. Structurally speaking however, a strategy is an expression composed of rewrite rules, combinators, and generic traversals.

7. labels – A strategy can be bound to a label for the purposes of abstraction.
In addition to the first-order constructs mentioned above, TL also supports the following higher-order constructs:

1. **higher-order strategies** – A higher-order strategy is a strategy that when applied to a tree will return a strategy rather than a tree. For example, when applied to a tree, a second-order strategy \( s^2 \) will yield a first-order strategy \( s^1 \). In general, the application of a strategy of order \( n \) to a term \( t \) will yield a strategy of order \( n - 1 \). For the purposes of uniformity, in this framework, a tree is considered to be a strategy of order 0.

2. **higher-order generic traversals** – A higher-order generic traversal can be thought of as a curried function that is parameterized on a higher-order strategy \( s^n \) (where \( n \) denotes the order of the strategy) and a tree \( t \). Its application to \( t \) yields a strategy of order \( n - 1 \). Higher-order generic traversals are very useful for creating specific strategies that are “tuned” the data occurring within a particular tree. In other words, they are a mechanism for dynamically generating strategies customized for a given input tree.

In the following sections we briefly describe each of the constructs mentioned above.

### 3.2 Tree/Term Notation

Let \( G = (N, T, P, S) \) denote a context-free grammar where \( N \) is the set of nonterminals, \( T \) is the set of terminals, \( P \) is the set of productions, and \( S \) is the start symbol. Given an arbitrary symbol \( B \in N \) and a string of symbols \( \alpha = X_1X_2...X_m \) where for all \( 1 \leq i \leq m : X_i \in N \cup T \), we say \( B \) derives \( \alpha \) iff the productions in \( P \) can be used to expand \( B \) to \( \alpha \). Traditionally, the expression \( B \Rightarrow \alpha \) is used to denote that \( B \) can derive \( \alpha \) in zero or more expansion steps. Similarly, one can write \( B \Rightarrow \alpha \) to denote a derivation consisting of one or more expansion steps.

In TL, we write \( B[[\alpha']] \) to denote an instance of the derivation \( B \Rightarrow \alpha \) whose resulting value is a parse tree having \( B \) as its root symbol. In TL, expressions of the form \( B[[\alpha']] \) are referred to as parse expressions. In the parse expression \( B[[\alpha']] \) the string \( \alpha' \) is an instance of \( \alpha \) because nonterminal symbols in \( \alpha' \) are constrained through the use of subscripts. Subscripted nonterminal symbols are referred to as schema variables or simply variables for short. TL also considers a schema variable (e.g., \( B_i \)) to be a parse expression in its own right. Within a rewrite rule all occurrences of schema variables having the same subscript denote the same variable.

Figure 14 shows a BNF grammar fragment describing a small portion of an imperative language. In the context of this grammar, the parse expressions \( stmt[[ id = 5 ]] \) and \( stmt[[ id_2 = 5 ]] \) both describe instances of the derivation \( stmt \Rightarrow id = 5 \).

When the specific structure of a parse expression is unimportant the parse expression will be denoted by variables of the form \( t, t_1, \ldots \) or variables of the form \( tree, tree_1, tree_2 \), and so on. Parse expressions containing no schema variables are called ground and parse expressions containing one or more schema variables are called non-ground. And finally, within the context of rewriting or strategic programming, trees as described here can and generally are viewed as terms. When the distinction is unimportant, we will refer to trees and terms interchangeably.
3.3 Conditional Rewrite Rules

Figure 15 defines the structure of TL rules in terms of an extended-BNF. The meta-symbols of this BNF are [], and ::= . Symbols enclosed in square brackets denote optional portions of a production. For example, rewrite rules in TL have the form lhs → rhs and may have optional labels and conditions associated with them.

```
rule ::= [ label : ] lhs → rhs [ if condition ]
label ::= identifier
lhs ::= a parse expression
rhs ::= a strategic expression whose evaluation yields a parse tree
```

Based on the tree grammar given in Figure 14, we can write the following condition-less rewrite rule:

\[ r_1 : stmt[[id_1 = 4 + 1]] → stmt[[id_1 = 5]] \]

This rule states that an assignment statement having the expression 4 + 1 as its right-hand side should be rewritten to an assignment statement having the constant 5 as its right-hand side.

3.3.1 Conditions

The conditional portion of a rule is a match expression consisting of one or more match equations. The symbol ≪, adapted from the ρ-calculus [6], is used to denote first-order matching modulo an empty equational theory. Let \( t_2 \) denote a ground tree and let \( t_1 \) denote a parse expression which may contain one or more schema variables. A match equation is denoted \( t_1 \ll t_2 \). A match equation is a boolean valued operation that produces a substitution \( \sigma \) as a by-product. A substitution \( \sigma \) binding schema variables to ground parse expressions is a solution to \( t_1 \ll t_2 \) if \( \sigma(t_1) = t_2 \) with = denoting a boolean valued test for syntactic equality.
A match expression is a boolean expression involving one or more match equations. Match expressions may be constructed using the standard boolean operators: ∧, ∨, ¬. A substitution σ is a solution to a match expression m iff σ(m) evaluates to true using the standard semantics for boolean operators.

Based on the tree grammar given in Figure 14, we can write the following conditional rewrite rule:

\[
r_2 : stmt_1 \rightarrow stmt_1'[id_1 = 5] \text{ if } stmt_1 \ll stmt_1'[id_1 = 4 + 1]
\]

The conditional rule \(r_2\) says that a statement \(stmt_1\) should be rewritten to the statement \(stmt_1'[id_1 = 5]\) only if the condition \(stmt_1 \ll stmt_1'[id_1 = 4 + 1]\) is satisfied. In other words, if \(stmt_1\) is an assignment statement whose right-hand side is the expression \(4 + 1\).

The rule \(r_3\) shown below gives a trivial example of a rule condition consisting of two match equations.

\[
r_3 : stmt_1 \rightarrow stmt_1'[id_1 = 5] \text{ if } stmt_1 \ll stmt_1'[id_1 = expr_1] \land expr_1 \ll expr_1[4 + 1]
\]

The conditional rule \(r_3\) says that a statement \(stmt_1\) should be rewritten to the statement \(stmt_1'[id_1 = 5]\) only if the condition \(stmt_1\) is an assignment statement whose right-hand side is \(expr_1\) and \(expr_1\) is \(4 + 1\).

### 3.3.2 Rule Application

The application of a conditional rewrite rule \(r\) to a tree \(t\) is expressed as \(r(t)\) where \(r\) is either an abstraction of a rewrite rule (i.e., a label) or an anonymous rule value e.g., \(lhs \rightarrow rhs\). We adopt a curried notation in the style of ML where application is a left-associative implicit operator and parentheses are used to override precedence or may be optionally included to enhance readability. For example, \(r t\) denotes the application of \(r\) to \(t\) and has the same meaning as \(r(t)\).

Let us consider the rules \(r_1\), \(r_2\), and \(r_3\) described in the previous sections. The application \(r_1 stmt_1[x = 4 + 1]\) yields \(stmt_1[x = 5]\) as do the applications \(r_2 stmt_1[x = 4 + 1]\) and \(r_3 stmt_1[x = 4 + 1]\). In contrast, the application \(r_1 stmt_1[y = 6]\) is said to fail and in TL will yield \(stmt_1[y = 6]\) as its result.

Let \(r : lhs \rightarrow rhs \text{ if condition}\) denote an abstract rule. In TL, the application of \(r\) to \(t\) proceeds as follows: First, the match-equation \(lhs \ll t\) is evaluated. If \(lhs \ll t\) evaluates to false, the rule application fails and \(t\) is left unchanged. Otherwise, \(lhs \ll t\) evaluates to true and the computation proceeds to the evaluation of the condition associated with \(r\). Again, if this condition evaluates to false, the rule application fails and \(t\) is returned unchanged. Otherwise the rule application succeeds and the value of \(rhs\) is returned.

### 3.4 Combinators

TL provides three binary combinators enabling (1) the sequential composition of strategies which is denoted by the semi-colon symbol, (2) the left-biased composition of strategies which is denoted by the symbol \(<+\), and (3) the right-biased composition of strategies which is denoted by the symbol \(\rightarrow\).

Let \(s_1\) and \(s_2\) denote two first-order strategies. The strategy \(s_1; s_2\) denotes the sequential composition of \(s_1\) and \(s_2\). When applied to a term \(t\) the strategy \(s_1; s_2\) will first apply \(s_1\) to \(t\) yielding \(t'\) and then apply \(s_2\) to \(t'\) yielding \(t''\).

The strategy \(s_1 <+ s_2\) denotes the left-biased composition of \(s_1\) and \(s_2\). When applied to a term \(t\) the strategy \(s_1 <+ s_2\) will first try to apply \(s_1\) to \(t\). If the application \(s_1\) succeeds, and produces \(t'\) as
its result, then \( t' \) is returned as the final result and \( s_2 \) is not used. However, if the application \( s_1 t \) fails, then the result of \( s_2 t \) is returned as the final result.

The strategy \( s_1 \Rightarrow s_2 \) denotes the right-biased composition of \( s_1 \) and \( s_2 \). Semantically speaking, \( s_1 \Rightarrow s_2 \) is equivalent to \( s_2 \lhd s_1 \).

In addition to the three binary combinators previously mentioned, TL also provides the unary combinators \( \text{transient} \) and \( \text{hide} \). The semantics of these combinators are described in Section 4.2.

### 3.5 Generic First-Order Traversals

TL supports a number of generic first-order traversals including: TDL, FIX_TDL, and TDL_B. The traversal TDL accepts a first-order strategy \( s \) and a tree \( t \) as input and performs a single top-down left-to-right traversal over \( t \) applying \( s \) to every sub-tree encountered. The traversal FIX_TDL accepts a first-order strategy \( s \) and a tree \( t_0 \) and performs the evaluation TDL \( s t_0 \) yielding \( t_1 \). If one or more rewrites occurred during the evaluation of TDL \( s t_0 \), then FIX_TDL will perform the evaluation TDL \( s t_1 \) yielding \( t_2 \). Additional evaluations of the form TDL \( s t_i \) will continue until a tree \( t_j \) is reached such that the evaluation TDL \( s t_j \) completes without a single rewrite being performed on \( t_j \). If such a tree \( t_j \) is found, then this is the value of the evaluation of FIX_TDL \( s t_0 \). Otherwise the evaluation of FIX_TDL \( s t_0 \) does not terminate.

The generic first-order traversal TDL_B is described in Section 4.4.

### 3.6 Higher-Order Rules and Strategies

In TL, a conditional rewrite rule of order \( n \) has the form:

\[
\text{label} : \text{lhs} \rightarrow s^n \text{ if condition}
\]

where \( s^n \) is a strategic expression whose evaluation yields a strategy of order \( n \). As was the case with first-order rules, the label and conditional portion of higher-order rules are optional.

The combinators in TL can be applied to first-order as well as higher-order strategies. For example, let \( s_1^n \) and \( s_2^n \) denote two order \( n \) strategies. The expressions \( s_1^n ; s_2^n \) and \( s_1^n \lhd s_2^n \) respectively denote the sequential and left-biased conditional composition of \( s_1^n \) and \( s_2^n \). For various practical reasons, TL imposes the restriction that only strategies having the same order may be composed with one another.

### 3.7 Higher-Order Generic Traversals

TL supports a number of generic higher-order traversals including: \( \text{seq_tdl} \) and \( \text{lcond_tdl} \). The traversal \( \text{seq_tdl} \) accepts a higher-order strategy \( s^n \) and a tree \( t_1 \) as its input and performs a top-down left-to-right traversal of \( t_1 \) applying the strategy \( s^n \) to each (sub)tree encountered. Let \( t_1, t_2, ..., t_m \) denote the trees encountered during the traversal of \( t_1 \). Let \( s_1^{n-1} \) denote the strategy obtained from applying \( s^n \) to the tree \( t_j \). Given these assumptions, the evaluation of \( \text{seq_tdl} s^n t_1 \) will produce the strategy

\[
s_1^{n-1} ; s_2^{n-1} ; ... ; s_m^{n-1}
\]

Similarly, the evaluation of \( \text{lcond_tdl} s^n t_1 \) will produce the strategy

\[
\text{23}
\]
Having described the basics of TL we are now in a position to discuss a strategic implementation of the class loader core.

4 A Strategic Implementation of the Class Loader Core

In this section we look at a strategic solution, written in TL, to an abstract version of the class loader core as defined in Section 1.2. In this abstract example, the structure of a class file has been greatly simplified and in several places its structure has even been altered. In spite of these changes, we nevertheless make the claim that, when seen from a strategic perspective, the abstractions below still contain the essence of the class loader core. This claim is based on our experience in successfully developing a strategic-based implementation of an actual class loader for the SSP. This implementation has been developed using the HATS system, an IDE for strategic programming supporting a restricted version of TL in dialect form. The HATS system is freely available [7].

Noteworthy characteristics of the class file structure described in Figure 16 include:

- Additional terminal symbols have been added to enable the class file structure to be described by a context-free grammar.
  - Constant pool entries have been enclosed in parenthesis.
  - The `@` symbol is used to tag absolute addresses belonging to $D_{HEAP}$.
  - The `:` symbol is used to tag object offset addresses belonging to $D_{Obj}$.
  - The `#` symbol is used to tag method table offset addresses belonging to $D_{MT}$.

- Explicit indexes have been given to the entries in the constant pool.

- The structure of a class file has been extended with a children list which is initially empty.

- Fields have been partitioned into a list of static fields and a list of instance fields.

- The methods section consists of a method table and a list of methods.

- Methods consist only of a method name. In particular, they do not contain a descriptor and they do not contain any bytecodes.

- All fields are tacitly assumed to be of type integer.

- Fields are denoted by a single index whose resolution yields the name of the field and the class in which it is declared.

- Address and offset units are words.

In the context of these constraints and alterations we present a strategic implementation of the class loader core. Figure 17 shows three abstract class files before class loading, and Figure 18 shows the same three class files after class loading. In order to construct a sufficiently rich example that is nevertheless small in size, the class file examples shown are not proper class files. For example, a super type makes a reference to its subtype.
Figure 16: An extended-BNF grammar describing a simplified application in terms of a list of class files
| This class | 1 |
| Super class | 19 |
| CP | (1, A)(2, 1.3)(3, x1)(4, 1.5)(5, x2)(6, 1.8)(7, 1.9)(8, a1)(9, a2)(10, 11.3)(11, B)(12, 11.13)(13, foo)(14, x3)(15, bar)(16, 1.14)(17, 1.13)(18, 1.15)(19, Obj) |
| Static fields | 6@- 4@- 16@- |
| Instance fields | 6:- 7:- |
| MT | |
| Methods | 17() 18() |

| This class | 3 |
| Super class | 19 |
| CP | (1, x1)(2, 3.1)(3, B)(4, x2)(5, 3.4)(6, x3)(7, 3.6)(8, b1)(9, 3.8)(10, b2)(11, 3.10)(12, foo)(13, 3.12)(14, f)(15, 3.14)(16, C)(17, 16.1)(18, 16.4)(19, A) |
| Static fields | 2@- 5@- 7@- |
| Instance fields | 9:- 11:- |
| MT | |
| Methods | 13() 15() |

| This class | 3 |
| Super class | 21 |
| Static fields | 2@- 5@- 7@- |
| Instance fields | 9:- 11:- |
| MT | |
| Methods | 13() 15() |

Figure 17: Three abstract class files prior to class loading
| This class | A           |
| Super class | B           |
| CP          | A.x1@0(3, x1)(4, A.x2@1)(5, x2)(6, A.a1:0)(7, A.a2:1)(8, a1) |
| Static fields | A.x1@0 A.x3@2 |
| Instance fields | A.a1:0 A.a2:1 |
| MT          | A.foo()     |
| Methods     | A.bar()     |

| This class | B           |
| Super class | A           |
| CP          | A.x1@3(3, C)(4, x2)(5, B.x2@4)(6, x3)(7, B.x2@5)(8, b1) |
| Static fields | B.x1@3 B.x3@5 |
| Instance fields | B.b1:2 B.b2:3 |
| MT          | B/foo()     |
| Methods     | B.bar()     |

| This class | C           |
| Super class | A           |
| CP          | A.x1@6(3, C)(4, x2)(5, C.x2@7)(6, x3)(7, C.x3@8)(8, c1) |
| Static fields | C.x1@6 C.x2@7 C.x3@8 |
| Instance fields | C.c1:2 C.c2:3 |
| MT          | A.foo#0 C.bar#1 |
| Methods     | C.f#2       |

Figure 18: The three abstract class files shown in Figure 17 after class loading
As described in Section 2.1, the goal of index resolution is to rewrite constant pool indexes into their symbolic references. In the abstract example that we are considering a constant pool entry has the form \((\text{index}_1, \text{data}_1)\), where \(\text{index}_1\) denotes the position of the entry and \(\text{data}_1\) denotes its value (e.g., an encoding of a symbolic reference or a symbolic reference). Conceptually speaking, our strategic approach to index resolution is as follows. For every constant pool entry \((\text{index}_1, \text{data}_1)\) we would like to create a rewrite rule of the form \(\text{index}_1 \rightarrow \text{data}_1\). Once this has been accomplished all that remains to be done is to exhaustively apply the resulting rules to all data indexes within the class file. We would like to point out that the structure of the constant pool entries \((\text{index}_1, \text{data}_1)\) is such that \(\text{index}_1\), the positional denotation of the entry, is not in-and-of-itself a data index. Data indexes occur in a variety of places throughout a class file such as within the description of fields, within the description of methods including their bytecodes, and within the data portion of constant pool entries.

The grammar in Figure 16 has been defined in such a way to enable an ordinary use of an index to be distinguished from a data index. In particular, all data indexes are derived from the nonterminal symbol \(d\). Thus, it is only in this structural context that index resolution should be performed. This constraint is captured by the parse expression \(d[[\text{index}_1]]\), yielding the rewrite rule \(d[[\text{index}_1]] \rightarrow d_1\).

Figure 19 gives an implementation of index resolution in TL. The behavior of the strategy index_resolution is as follows. When applied to a class file structure \(\text{class}_0\) the strategy index_resolution will first evaluate the strategic expression \(\text{seq_tdl cp_normalize class}_0\). Within this expression, the strategy \(\text{seq_tdl}\) is a higher-order generic traversal that will traverse a term in a top-down left-to-right (tdl) fashion. In this case, the term being traversed is \(\text{class}_0\). The fact that \(\text{seq_tdl}\) is higher-order means that it expects to apply a higher-order strategy to the sub-terms of the term it is traversing. In this case, the higher-order strategy being applied is \(\text{cp_normalize}\), a second-order strategy that converts a constant pool entry of the form \(\text{c_entry}[[ (\text{index}_1, \text{d}_1) ]] \rightarrow \text{d}[[\text{index}_1]] \rightarrow d_1\). When applied to the entries of the constant pool of \(\text{class}_0\) a number of instances of the rule \(\text{d}[[\text{index}_1]] \rightarrow d_1\) will be generated. These rule instances are then composed by \(\text{seq_tdl}\) using TL’s sequential composition operator. This composition is part of the semantics of \(\text{seq_tdl}\) – which sequentially composes the results generated generates from its tdl traversal. The resulting first-order strategy is of the form \(r_1; r_2; \ldots; r_n\) where \(r_i\) is the instance of \(\text{d}[[\text{index}_1]] \rightarrow d_1\) corresponding to the \(i^{th}\) constant pool entry. This first-order strategy is then exhaustively applied to \(\text{class}_0\) in a top-down left-to-right fashion by the first order generic traversal \(\text{FIX_TDL}\). The result is that all data indexes are rewritten to their symbolic references.

\[
\begin{align*}
\text{index_resolution} & : \text{class}_0 \rightarrow \text{FIX_TDL (seq_tdl cp_normalize class}_0\text{) class}_0 \\
\text{cp_normalize} & : \text{c_entry}[[ (\text{index}_1, \text{d}_1) ]] \rightarrow \text{d}[[\text{index}_1]] \rightarrow d_1
\end{align*}
\]
4.2 Static Field Address Calculation in TL

As described in Section 2.2, the goal of static field address calculation is to assign each static field in an application a unique absolute address taken from the address space $D_{H, E, A, P}$. In TL, this can be accomplished with a strategy that makes use of the strategic combinators $\text{transient}$ [26][27] and $\text{hide}$ [28][29]. Both of these combinators are unique to TL.

When applied to a strategy $s$, the $\text{transient}$ combinator has the effect of “erasing” $s$ after the first successful application of $s$. Thus, the $\text{transient}$ combinator can be used to create a strategy that can be applied at most once. For example, let $s_1$ denote the strategy $\text{transient}(\text{addr}[[0]] \rightarrow \text{addr}[[1]])$. The strategic expression $TDL ~ s_1 ~ \text{class}_0$ states that the term $\text{class}_0$ should be traversed in a top-down left-to-right fashion and that the current value of strategy $s_1$ should be applied to every term encountered during this traversal. Due to the use of the $\text{transient}$ combinator in $s_1$, the strategic expression $TDL ~ s_1 ~ \text{class}_0$ will have the effect of rewriting the first term matching $\text{addr}[[0]]$ to $\text{addr}[[1]]$ and will leave unchanged all other terms.

Generalizing this example, let $s_i$ denote a strategy of the form $\text{transient}(\text{addr}[[0]] \rightarrow \text{addr}[[i]])$, and let $s_{1..n}$ denote a strategy of the form $s_1; s_2; ...; s_n$. The strategic expression $TDL ~ s_{1..n} ~ \text{class}_0$ will rewrite the first occurrence of $\text{addr}[[0]]$ to $\text{addr}[[1]]$, the second occurrence of $\text{addr}[[0]]$ to $\text{addr}[[2]]$, and the $n^{th}$ occurrence of $\text{addr}[[0]]$ to $\text{addr}[[n]]$. Suppose we are given a Java application whose class files collectively contain $m$ static fields, all of which are of type integer and whose initial default address has been set to 0. When controlled properly, the application of a strategy of the form $s_{1..m}$ can be used to correctly assign a unique address to each static field in the application. In spirit, this is the transformational effect that we want to accomplish. However, for a variety of reasons, in practice it is difficult to attempt to construct such a strategy directly. Thus, we will use the $\text{hide}$ combinator to construct a slightly different strategy whose net effect is equivalent to $s_{1..m}$.

In strategic programming, the left-biased choice combinator $\langle \rangle$ is used to specify the conditional application of two or more strategies. When applied to a term $t$, the strategy $s_1 \langle \rangle s_2$ specifies that first the application of $s_1$ to $t$ should be attempted. If this application succeeds and yields $t'$, then the result of $(s_1 \langle \rangle s_2)$ $t$ is $t'$. On the other hand, if the application of $s_1$ to $t$ fails, then the left-biased choice combinator indicates that the application of $s_2$ to $t$ should be tried next. In light of this, let us consider the strategy $\text{hide}(s_1) \langle \rangle s_2$. The $\text{hide}$ combinator is a combinator that restricts the ability of the left-biased (or right-biased) choice combinator to observe whether or not the application of $s_1$ has succeeded or failed. More specifically, the $\text{hide}$ combinator always gives the left-biased choice combinator the impression that the application of $s_1$ has failed. Thus, the strategy $\text{hide}(s_1) \langle \rangle s_2$ is equivalent to $s_1; s_2$.

When considered in isolation, the $\text{hide}$ combinator is not very interesting. However, when combined with the $\text{transient}$ combinator it becomes possible to construct strategies having interesting behaviors, such as a strategy that implements a sum. For example, consider the following strategy:

$$\text{sum} = \begin{cases} 
\text{hide}(\text{addr}[[i]]) \rightarrow \text{addr}[[i + 1]] \langle \rangle \text{transient}(\text{addr}_1 \rightarrow \text{addr}_1) \langle \rangle \\
\text{hide}(\text{addr}[[i]]) \rightarrow \text{addr}[[i + 1]] \langle \rangle \text{transient}(\text{addr}_2 \rightarrow \text{addr}_2) \langle \rangle \\
\text{hide}(\text{addr}[[i]]) \rightarrow \text{addr}[[i + 1]] \langle \rangle \text{transient}(\text{addr}_3 \rightarrow \text{addr}_3) 
\end{cases}$$
When applied to a term \( t \), the strategy \( \text{sum} \) will increment the first \( \text{addr} \) it encounters by one, the second \( \text{addr} \) it encounters by two (i.e., \( 1 + 1 \)), and the third \( \text{addr} \) it encounters by three (i.e., \( 1 + 1 + 1 \)). All remaining instances of \( \text{addr} \) encountered will be incremented by three. The informal explanation of this is as follows. Within \( t \), when applied to the first occurrence of \( \text{addr} \), the first \( \text{hide} \) encapsulated rule in \( \text{sum} \) will apply, incrementing the address by one. Due to the encapsulation of the \( \text{hide} \) combinator, the conditional operator \(<+\) immediately to the right of the \( \text{hide} \) strategy is led to believe that the application of \( \text{hide}(\text{addr}[[i]] \rightarrow \text{addr}[[i + 1]]) \) failed. Thus, the application of the next strategy within \( \text{sum} \) is attempted, which in this case is \( \text{transient}(\text{addr}_1 \rightarrow \text{addr}_1) \). The rule \( \text{addr}_1 \rightarrow \text{addr}_1 \) is an identity that rewrites the term \( \text{addr}_1 \) to itself. From the perspective of \(<+\) the application of the \( \text{transient} \) encapsulated rule succeeds, completing the application of \( \text{sum} \) to \( \text{addr} \). However, since \( \text{transient} \) strategies can only be applied once, all future applications of this first \( \text{transient} \) strategy will fail, which in the context of \( \text{sum} \) will cause the application of \( \text{sum} \) to move on to its next rule. Thus, when \( \text{sum} \) is applied to a second \( \text{addr} \), the first two \( \text{hide} \) encapsulated rules will apply, after which the second \( \text{transient} \) encapsulated rule is encountered (for the first time), which again completes the application of \( \text{sum} \) to the second \( \text{addr} \). By similar reasoning, the application of \( \text{sum} \) to a third \( \text{addr} \) will result in three \( \text{hide} \) encapsulated increments.

\[
\begin{align*}
\text{static_addresses} & : \quad \text{app}_0 \rightarrow \text{TDL}(\text{lcond_tdl sfield_sum app}_0) \text{ app}_0 \\
\text{sfield_sum} & : \quad \text{sfield}_0 \rightarrow \\
& \quad \text{hide}(\text{sfield}[[\text{key}_1 @ \text{addr}_1]] \rightarrow \text{sfield}[[\text{key}_1 @ \text{addr}_1 + 1]]) <+ \text{transient}(\text{sfield}_1 \rightarrow \text{sfield}_1)
\end{align*}
\]

Figure 20: A TL strategy for absolution address calculation

Figure 20 gives a TL implementation of static field address calculation. The absolute address for static fields are realized via a strategic sum that is based on the increment technique described by the \( \text{sum} \) strategy discussed previously. In particular, the higher order strategy \( \text{sfield_sum} \) performs a sum that applies only to static fields. Within the body of \( \text{static_addresses} \), the higher-order strategic expression \( \text{lcond_tdl sfield_sum app}_0 \) will traverse \( \text{app}_0 \) in a tdl fashion and apply the strategy \( \text{sfield_sum} \). This will produce one instance of the strategy

\[
\text{hide}(\text{sfield}[[\text{key}_1 @ \text{addr}_1]] \rightarrow \text{sfield}[[\text{key}_1 @ \text{addr}_1 + 1]]) <+ \text{transient}(\text{sfield}_1 \rightarrow \text{sfield}_1)
\]

for each static field encountered. These strategy instances are then combined using the left-biased choice combinator. The resulting composition is an sfield sum which is then applied to \( \text{app}_0 \) using the generic traversal \( \text{TDL} \). This has the effect of assigning a unique absolute offset to each static field in \( \text{app}_0 \).

### 4.3 Instance Field Offset Calculation in TL

Instance field offset calculation (see Section 2.3) is similar to static field address calculation. The primary difference is that the assignment of offset addresses is constrained by the subtype (i.e., inheritance) relationships between the class files within an application. In static field address calculation, the static fields of all classes in the application could be collected (in any order) and aggregated into a sum, which could then be applied to the entire application (in the same order as collected). In instance field offset
calculation, the instance fields of each class in an inheritance chain must be collected according to the order/position of the class in the inheritance chain. The resulting sum must then be applied only to the instance fields of that chain.

In TL, there are several ways to construct strategies whose application is restricted to individual inheritance chains. The approach taken in this article requires that an application first be restructured so that the new structure explicitly reflects the inheritance hierarchy of the class files. This is accomplished by adding a children element to each class file (see Figure 16). This children structure denotes a list of class files and creates the possibility of restructuring the class files from an application (which are initially list form) into an inheritance tree. After this has been accomplished an iterative process can be specified whereby a strategy realizing a partial sum is created using the instance fields belonging to a given class file \texttt{class1} and the resulting partial sum strategy is applied to all the classes belonging to the inheritance tree having \texttt{class1} as its root (i.e., \texttt{class1} and all its descendants). During the course of a top-down traversal, each class file will in turn become the root of its own inheritance (sub)tree and have a partial sum created for it. The cumulative result is that each instance field will eventually be assigned a proper offset address (i.e., a fully totaled sum).

<table>
<thead>
<tr>
<th>Instance Offsets</th>
<th>\texttt{app1} \rightarrow \texttt{app3}</th>
</tr>
</thead>
<tbody>
<tr>
<td>if</td>
<td>\texttt{app2} \llap{\textless} \texttt{TDL} (seq_tdl create_hierarchy \texttt{app1}) \texttt{app}[[ { \text{Obj} \ Obj } ]]</td>
</tr>
<tr>
<td>∧</td>
<td>\texttt{app3} \llap{\textless} \texttt{TDL} sum_offsets \texttt{app2}</td>
</tr>
</tbody>
</table>

| Create Hierarchy | \texttt{class1} \rightarrow \texttt{class}[[ \{ \text{id2 id3 info2 children2} \} ]\rightarrow \texttt{class}[[ \{ \text{id2 id3 info2 children2 \texttt{class1}} \} ]] |
| if              | \texttt{class1} \llap{\textless} \texttt{class}[[ \{ \text{id1 id2 info1 children1} \} ]] |

| Sum Offsets | \texttt{class0} \rightarrow \texttt{TDL} (lcond_tdl partial_sum instance1 \texttt{class0}) \texttt{class0} |
| if          | \texttt{class0} \llap{\textless} \texttt{class}[[ \{ \text{class id1 parent id1 cp1 statics1 instance1 methods1 children1} \} ]] |

| Partial Sum | \texttt{class0} \rightarrow \texttt{TDL (lcond_tdl local ifield sum class0 class0)} |
| Local Ifield Sum | \texttt{ifield0} \rightarrow |
|                | \texttt{hide (ifield[[key1 : addr1]] \rightarrow ifield[[key1 : addr1 + 1]] ) \rightarrow transient(ifield1 \rightarrow ifield1)} |

Figure 21: Offset address calculation

Figure 21 gives a TL strategy that implements the approach to instance offset calculation just described. When applied to \texttt{app1}, the strategy \texttt{instance offsets} will first restructure \texttt{app1} into an inheritance tree. The evaluation of the strategic expression \texttt{seq_tdl create_hierarchy} \texttt{app1} will perform a top-down left-to-right traversal on \texttt{app1} and apply the higher-order strategy \texttt{create hierarchy} to each class file encountered. The application of \texttt{create hierarchy to class1} will produce a first-order strategy that places \texttt{class1} into the children list of its parent class. Notice that in the strategy \texttt{create hierarchy}, \texttt{id1} and \texttt{id2} respectively denote the class name and parent class name of \texttt{class1}. By definition, the parent class of \texttt{class1} is that class which has \texttt{id2} as its class name. Thus, in \texttt{create hierarchy} the strategy

\[
\texttt{class}[[ \{ \text{id2 id3 info2 children2} \} ]\rightarrow \texttt{class}[[ \{ \text{id2 id3 info2 children2 \texttt{class1}} \} ]]
\]

will place \texttt{class1} into the children list of its parent class.
For each class in $app_1$ such a first-order strategy is created and the resulting strategies are sequentially composed. The resulting composition is then applied in a top-down left-to-right fashion to an application structure consisting of the single class $Obj$, which is initially empty (i.e., $Obj$ contains no constant pool, no fields, no methods, and no children). This application has the effect of growing an inheritance tree rooted at $Obj$. For example, first the children of $Obj$ will be inserted into the children list of $Obj$. In turn, the children of $Obj$ will have their children inserted into their children list, and so on. The resulting structure is then bound to $app_2$ via a match equation.

After the application has been restructured into an inheritance tree, the calculation of instance field offsets can begin. In the strategy $instance offsets$, the evaluation of the strategic expression $TDL sum_offsets app_2$ will traverse the inheritance tree $app_2$ in a top-down left-to-right fashion and apply the strategy $sum_offsets$ to each class file encountered. In turn, the strategy $sum_offsets$ will traverse the instance fields of the class file $class_1$ to which it is applied and create an instance of $local_ifield_counter$ for each field encountered. The instances of $local_ifield_counter$ are then conditionally composed and the resulting strategy is applied to in a top-down left-to-right fashion to the inheritance tree rooted at $class_1$. This has the effect of (1) assigning proper (i.e., completed) offsets for the instance fields in $class_1$, and (2) assigning partially completed offsets for the instance fields of all the classes which are descendants of $class_1$. In general, the partially completed offsets for instance fields local to a given $class_i$ are completed when the strategy $sum_offsets$ is applied to $class_i$ (i.e., it is treated as the root of an inheritance tree).

### 4.4 Method Table Construction in TL

Method table construction (see Section 2.4) is similar to instance field offset calculation in the sense that strategies are applied along inheritance chains. In the case of method table construction the goal is to construct a method table for each class within an application. The general algorithm implemented is as follows. One begins at the class $Obj$ with an empty method table. This table is then propagated to all the descendants of $Obj$ after which, method table construction begins for the children of class $Obj$. Let $class_1$ denote an arbitrary child of $class Obj$. The methods declared in $class_1$ are “added” to the method table of $class_1$ as well as to the method tables of all the descendants of $class_1$. This distribution represents the methods that are initially inherited by the descendants of $class_1$. In general, the methods in $class_i$ are added to the method table of $class_i$ and all of its descendants. The “addition” of a method $m$ to the method table of $class_i$ can take one of the following three forms:

1. A method table entry $m'$ is encountered corresponding to the method $m$. This means that $m'$ has been redefined by $m$ in $class_i$. In this case, $m$ replaces (overwrites) the entry for $m'$.

2. The last entry of a (non-empty) method table is reached without encountering an entry corresponding to $m$. This means that, $m$ is a new (i.e., previously unseen) method declared in $class_i$. In this case, a new entry is added to the end of the method table and its offset is assigned the value of the previous offset plus one.

3. An empty method table is encountered. In this case, an entry for $m$ is added to the method table and given an offset of zero.

32
Figure 22: Method table construction

Figure 22 shows how the method table construction strategy described can be implemented in TL. When applied to a method declaration, the strategy `insert_method` creates a transient strategy that, though the use of the left-biased choice combinator, captures the three ways a method can be added to a method table. The rule

\[
mt[[id_3.id_2 \# addr_2 mt_2]] \rightarrow mt[[id_1.id_2 \# addr_2 mt_2]]
\]

accounts for the case where a local method definition overwrites an inherited method definition. In this case, id_3 denotes the most recent ancestor where the method id_2 has been declared and id_1 denotes the name of the current class in which the method is being redeclared. The rule

\[
mt[[id_3.id_4 \# addr_2]] \rightarrow mt[[id_3.id_4 \# addr_2 id_1.id_2 \# addr_2 + 1]]
\]

accounts for the case where a previously unseen method is declared and must therefore be added to the end of the method table with an offset of addr_2 + 1. And finally, the rule

\[
mt[[ ]] \rightarrow mt[[id_0.id_1 \# 0]]
\]

accounts for the somewhat special case where a method is added to an empty method table. In this case the offset address is set to 0. Notice that the aggregation of the above rules needs to be encapsulated within a `transient` in order to assure that a method \( m \) will only be added to a method table once. For example, it would be incorrect to overwrite an existing method and also add a new (i.e., duplicate) entry to the end of the same method table.

Within the strategy `add_methods`, the evaluation of the strategic expression `seq.tdl insert_method method_list` will result in the creation of a method table insertion strategy for each method in `method_list`, which is the list containing the methods that are declared in `class_1`. The insertion strategies are sequentially composed by `seq.tdl` and the resulting strategy is ready to be applied to a method table. Let \( s \) denote this strategy. The trick that needs to be worked out now is how to apply this value of \( s \) to the method table in `class_1` as well as the method tables of every class which is a descendant of `class_1`. The problem is that \( s \) contains transient strategies and the moment a transient strategy applies the value
of s will be forever changed. For example, adding an entry to the method table of class1 will change
s so that this element cannot in the future be added to the method tables of any of the descendants
of class1. To solve this problem what we need is some way of making a copy of the current value of
s (i.e., the value before any transient strategies have been applied). The first-order generic traversal
TDL.B does just that! In general, the evaluation of a strategic expression of the form TDL.B s t will
perform a top-down left-to-right traversal over the term t and do the following: First, s is applied to
the current term t producing a (possibly) new term t' and a (possibly) new strategy s'. Next, a copy
of the strategy s' is applied to each of the children of t', at which point the process repeats until the
entire tree is traversed. As a result the evaluation of the strategic expression

\[ TDL.B(seq_tdl insert_method method_list1) \textit{class1} \]

will correctly insert the methods declared in method_list1 into the method table of class1 as well as
in the method tables of all the descendants of class1. And finally, the strategy \textit{mt_construction}, when
applied to an application \textit{app1} that is in the form of an inheritance tree, will create the proper method
tables for each class in \textit{app1}. It accomplishes this by traversing \textit{app1} in a top-down left-to-right fashion
and applying the strategy \textit{add_methods} to every inheritance tree encountered.

4.5 Inter-class Absolute Address and Offset Address Distribution in TL

At this point, all data indexes within the application have been resolved to symbolic references, all
static fields in the application have been assigned absolute addresses in \( D_{HEAP} \), all instance fields in
the application have been assigned offset addresses in \( D_{OBJ} \), and all methods in the application have
been assigned method table offset addresses in \( D_{MT} \). Given these preconditions, inter-class absolute
address and offset address distribution concerns itself with the distribution of the aforementioned address
values to their corresponding symbolic references in constant pool entries. Note that such references
are not particularly constrained by inheritance chains. That is, a class file belonging to one inheritance
chain may reference static fields, instance fields, and methods declared in a class file belonging to another
inheritance chain.

Figure 23 shows a TL implementation of \textit{inter-class absolute address and offset address distribution}.
The evaluation of the strategic expression \textit{lcond_tdl collect_ifields app1} will create an instance of the rule

\[ c\_entry[ (index1, key1) ] \rightarrow c\_entry[ (index1, key1 : addr1) ] \]

for each instance field in the application \textit{app1}. This rule adds the offset associated with the instance
field \textit{key1} to a constant pool entry containing the symbolic reference \textit{key1}). These rule instances are
composed using the left-biased choice combinator and the resulting strategy is then applied to \textit{app1} using
the generic traversal \textit{TDL}. The effect is that all constant pool entries containing symbolic references to
instance fields will be updated so they also contain the corresponding offset address for that instance
field. The result of this transformation is then bound to \textit{app2} via a match equation. Next the absolute
addresses for all static fields is \textit{app2} is distributed by the same mechanism that was used to distributed
instance field offsets. The result is then bound to \textit{app3} via a match equation. And finally, method table
offsets are distributed, completing the class loader core as defined in Section 1.2.
5 Verification and Validation

One motivating factor in the development of TL in general and the SSP specifically is the attainment of strong evidence of correctness. In this section we present current efforts to construct a framework for proving the correctness of TL transformations using the automated theorem prover ACL2.

The goal with respect to the SSP class loader is to prove formally and automatically that the TL implementation of the class loader preserves the properties identified in Section 1.2. To this end, we are beginning to model the behaviors of strategies, traversals, combinators, and conditional rewrites in ACL2. The work described here is only the initial steps towards proving the correctness of the TL implementation of the class loader core. The long-range goal of this work is to reason not only about specific transformations, but also about the internal mechanisms of TL and transformation systems in general. ACL2 has the capability to reason about combinators and traversal strategies, and this reasoning can be reused in other applications that utilize transformation-oriented programming.

5.1 The ACL2 Theorem Prover

ACL2 [8] [9] is a first order, quantifier-free mathematical logic based on recursively defined total functions. It is also a programming language based on the applicative subset of Common Lisp in which users can build executable models of software systems and prove that these models have certain properties. To use ACL2, a user first builds an executable model by writing functions in the ACL2 language. Before a function definition is accepted, ACL2 must prove that the function is total, i.e., it eventually terminates for any input. Once a function is accepted, a user may execute the function to test it or prove theorems about the function.

Theorems are specified using the construct `defthm`. While ACL2's theorem prover is fully automatic, it is usually necessary for a user to supply lemmas to guide the proof. Once a theorem has been proved, it can be used in subsequent proofs. Theorem conjectures have the following general form:

```
(defthm theorem-name
  (implies cond1
    (equal expression1 expression2))
  :rule-classes :rewrite)
```
To prove theorems, ACL2 uses six proof techniques: simplification, elimination of destructors, use of equivalences, generalization, elimination of irrelevance, and induction. The two most important techniques are simplification and induction. After proving a theorem, ACL2 will store the result as a rewrite and use it during simplification. In this case, whenever ACL2 encounters expression1 to expression2 given that cond1 is true.

To prove a theorem, \( T(n) \), by classical induction, we have to show as a base case that \( T(0) \) holds, then as the induction step that \( T(n) \rightarrow T(n + 1) \). The induction used in ACL2 restates the classical one: to prove \( T(n) \) we have to show that \( T(0) \) holds, then as the induction step we have to show that \( (n \neq 0) \) and \( T(n - 1) \rightarrow T(n) \). Thus, ACL2 attempts to prove a theorem \( T(n) \) by induction from a smaller instances of the theorem, \( T(n - 1) \).

### 5.2 Modelling TL in ACL2

We are beginning to model the semantics of TL in ACL2. Our approach is to model the class loader as a function that takes a Java application (set of Java class files) as input and produces a ROM image as an output. The goal is to show the equivalence of these two representations. To prove the equivalence, we create a function that maps a Java application \( APP \) to a semantic expression \( E_{APP} \). A second semantic function takes a ROM image and maps it to a semantic expression \( E_{ROM} \). Our conjecture is that \( E_{APP} \) is equivalent to \( E_{ROM} \) modulo class loading. Rather than show this equivalence for some finite number of test cases, we want to prove that equivalence holds for any valid Java application. We begin by assuming that the Java application and the transformation rules have corresponding tree representations that are inputs to the TL model. The model supports the combinators \( FIX_{TDL}, TDL, \) and \( transient \); we are currently working on supporting the remaining combinators.

ACL2 requires that functions be total. It is therefore impossible to directly model some computational systems. For example, it is not possible to directly model the Java virtual machine since it is possible to write Java programs that do not terminate. The approach to modelling the TL in ACL2 is based on the approach taken to model possibly non-terminating systems \([12] [17] [13] [14]\). In this approach, a system is described in terms of states and a state transition function. (This approach has been used to verify parts of implementations of the Java Virtual Machine \([12] [17][13]\).

A state transition function takes a state as input and returns a new state. The new state is derived from the input state by advancing the system by some number of atomic steps. For example, in the Java virtual machine models, a single step is the execution of a single byte code.

We define a step in the ACL2 model of TL to be the application of a single conditional rewrite rule to a specific node in a tree. Our transition function has two inputs: an input state and a number representing how many steps should be taken to produce the output state. Recall that the application of a first-order strategy to a tree generally defines a number of rewrites on that tree. Thus, given a proper number of steps, our transition function implements a strategy.

A state of TL is modeled as a tuple \( <CF_I, T, C, TP, CF_P, H> \) where \( CF_I \) is an input class file; \( T \) is a set of rewrite rules; \( C \) is a control strategy that controls the application of the transformation rules to the class file; \( TP \) is a rewrite pointer that keeps track of the next rewrite rule to be applied; \( CF_P \) is a Class file pointer that keeps track of the class file entry to which the current rewrite rule will be applied; and a halt flag, \( H \), to show when an execution session ends.
The SSP class loader can be viewed as a function that takes Java application \( \text{app}_0 \) as input and produces a ROM image \( C_{RFOM} \) as output. In Section 2 this core functionality has been decomposed into a sequence of canonical forms. The five canonical forms correspond to index resolution, static field address calculation, instance field offset calculation, method table construction, inter-class absolute address and offset address distribution.

Given a set of state transition functions \( STF_{form_n} \) that convert intermediate applications from one canonical form to another, the sequence of intermediates is given below:

\[
\begin{align*}
Form_1 &= STF_{form_1}(CF_0, nstep_1) & \text{Index Resolution} \\
Form_2 &= STF_{form_2}(Form_1, nstep_2) & \text{Static Field Address Calculation} \\
Form_3 &= STF_{form_3}(Form_2, nstep_3) & \text{Instance Field Offset Calculation} \\
Form_4 &= STF_{form_4}(Form_3, nstep_4) & \text{Method Table Construction} \\
C_{RFOM} &= STF_{form_5}(Form_4, nstep_5) & \text{Inter-class Absolute Address and Offset Address Distribution}
\end{align*}
\]

Here \( STF_{form_1} \) represents the transition function that given the correct number of steps \( nstep_1 \) converts an input class file \( CF_0 \) into the first canonical form \( Form_1 \). Similarly, \( STF_{form_2} \) converts a file from the first to the second canonical form. Each transition function will apply a set of rewrite rules to the state according to the specified control strategy. After the appropriate number of steps have been executed, the halt flag, \( H \), is set. The resulting application is stored. This application represents either the resulting ROM image or one of the intermediate forms.

5.3 Verification of the Correctness of the Transformation Rules

In this section, we sketch the proof of the correctness of the rewrite rules that embody the functionality of the SSP class loader. A crucial part of the verification effort is to define a semantic function that determines the equivalence of the input and the output of each transition function. Therefore, for each transition function, there is a semantic function, \( SemanticEquiv_i \). Our main conjecture is as follows:

\[
\forall(CF_0) SemanticEquiv(CF_0) = SemanticEquiv(STF_{form*}(CF_0), nstep*),
\]

which can be proved using transitivity of the following sequence of conjectures:

\[
\begin{align*}
\forall(CF_0) SemanticEquiv(CF_0) &= SemanticEquiv_1(STF_{form_1}(CF_0, nstep_1)) \\
&= SemanticEquiv_2(STF_{form_2}(STF_{form_1}(CF_0, nstep_1)), nstep_2) \\
&\quad \ldots \\
&= SemanticEquiv_n(STF_{form*}(CF_0, nstep*))
\end{align*}
\]

where \( STF_{form*} \) is the composition of the individual transition functions and \( number* \) is the total number of steps needed in the transformation of \( CF_0 \) to \( C_{RFOM} \). This allows the proof to be constructed incrementally, and therefore, reduces the complexity of the proof.

The goal of the transition function \( STF_{form_1} \) is to remove all indirection in the constant pool sections of the class files in \( CF_0 \), i.e., perform index resolution. We will also define the accompanied \( SemanticEquiv_1 \) function. Our goal in the example is to prove the following conjecture:
$\text{SemanticEquiv}(CF_0) = \text{SemanticEquiv}_1(\text{STF}_{form_1}(CF_0, nstep_1))$

In the proofs shown below, we present the $\text{SemanticEquiv}_1$ function. We prove that this function is correct, i.e., it has some desired property. Then we show the conjecture that is required to prove the TL implementation computes an equivalent value.

The goal in this example is to establish a transformational environment that is capable of resolving the pointers in the second column of the table, i.e., to replace each index with the string to which it points. The model shown here is greatly simplified from a true SSP class file. In our current ACL2 model, we represent the constant pool as a list of pairs. Each pair has an index and a value. This format illustrates the notion of indirection within the constant pool. As shown below, the first entry has index 1, and its value is the string “Hello”.

\[
\text{CP} = ((1 \text{ “Hello”}) \\
(2 \text{ “World”}) \\
(3 2) \\
(4 3))
\]

Each $\text{CP}$ entry consists of two components: the first is a natural number, and the second is either a string (Utf8) or a natural number that is smaller than the first component. In this case, the second component is a pointer to some previous entry in the pool. We require that such references be strictly decreasing, that is, such indirection must point to an earlier entry in the table. This simplifies the proof of termination of the function that follows the resolution chain.

To resolve $\text{CP}$, a rule is needed for each entry of $\text{CP}$ that contains a pair ($i$ $j$). This rule relates $i$ and $j$ in a specific context. A second-order transformation rule simplifies the resolution of $\text{CP}$. The rule $\text{TR}_1 = (i$ $j) \rightarrow (x$ $i) \rightarrow (x$ $j)$ generates as set of rules that transform $\text{CP}$. $\text{TR}_1$ states that for each entry in the table, create a new first-order rule that replaces the right-hand side of the pair. The generated rules for $\text{CP}$ are:

\[
\begin{align*}
\text{TR}_{1.0} &= (x$ 1) $\rightarrow (x$ “Hello”) \\
\text{TR}_{1.1} &= (x$ 2) $\rightarrow (x$ “World”) \\
\text{TR}_{1.2} &= (x$ 3) $\rightarrow (x$ 2) \\
\text{TR}_{1.3} &= (x$ 4) $\rightarrow (x$ 3)
\end{align*}
\]

Rule $\text{TR}_{1.3}$, for example, says to replace any entry in the table that has a right-hand value of 4 with an entry that has the same left-hand value, but the right-hand value is set to 3.

The use of the $\text{TDL}$ strategy is not enough to resolve all the pointers in $\text{CP}$. Applying all four of the transformation rules to the table once leaves the final table entry as $(4$ 2). Thus, the $\text{TDL}$ strategy must be applied as many times as necessary to have all the pointers in the table resolved. This is the $\text{FIX}_T\text{DL}$ strategy.

The function $\text{fixStrategy}$ simulates the behavior of the $\text{FIX}_T\text{DL}$ strategy in TL. This function takes as input a class file and generates dynamically the corresponding transformation rules. Thereafter, the transformation rules are exhaustively applied to the class file until all the pointers are resolved. The
function \textit{fixStrategy} achieves this by calling the function that implements the \textit{TDL} strategy repeatedly until there are no more pointers to resolve.

To verify the transformation rules, we define a semantic function, \textit{resolveLinks}, which copies a table replacing the second component of every entry by the (Utf8) string at the end of the pointer chain. This function uses the function \textit{(getConstant n cp)}, which takes a natural number \textit{n} and a constant pool table \textit{cp}. \textit{n} is an index that is followed until a (Utf8) string is reached. The definition of the function \textit{getConstant} in ACL2 is as follows.

\begin{verbatim}
(defun getConstant (n cp)
  (let ((temp (assoc n cp)))
    (cond ((null temp) nil) ; return nil if no entry
          ((stringp (cadr temp)) (cadr temp)) ; done if utf8
            ((or (not (natp n)) ; nil if table is broken
                 (not (natp (cadr temp)))
               (<= n (cadr temp)))
             nil)
            (t (getConstant (cadr temp) cp))))

The function \textit{resolveLinks} calls the function \textit{resolveLinks1}, which iterates down \textit{CP} replacing each second component by its associated string value from the original table.

\begin{verbatim}
(defun resolveLinks1 (tail cp)
  (cond ((endp tail) nil)
        (t (cons (list (car (car tail))
                    (getConstant (car (car tail)) cp))
            (resolveLinks1 (cdr tail) cp))))

(defun resolveLinks (cp) (resolveLinks1 cp cp))
\end{verbatim}

The following theorem verifies the function \textit{resolveLinks}:

\begin{verbatim}
(defthm getConstantResolveLinks
  (implies (and (natp n)
                  (alistp cp))
           (equal (getConstant n (resolveLinks cp))
                  (getConstant n cp))))
\end{verbatim}

ACL2 is not able to prove this theorem directly. In order to prove the theorem, it is first necessary to show that the function \textit{resolveLinks1} computes the same thing that \textit{resolveLinks1} does. The following lemma states that if we are given an index (a natural number \textit{n}) and a table (the association list \textit{tail}), then looking up the index in a resolved table is the same as extracting the constant from the original table.
An association list is a list of pairs. The first element of the pair is a key, and the second is the value. The function \texttt{assoc} takes a key and an association list and returns the first pair that matches the key. To prove \texttt{assocResolveLinks1}, ACL2 chooses an induction schema suggested by the definition of \texttt{assoc}. The essential part of the \texttt{assoc} function is given below.

\begin{verbatim}
(DEFUN ASSOC (X ALIST)
  (COND ((ENDP ALIST) NIL)
        ((EQUAL X (CAR (CAR ALIST))) (CAR ALIST))
        (T (ASSOC X (CDR ALIST)))))
\end{verbatim}

The induction has two base cases and one induction step. The base case correspond to the conditions \texttt{(ENDP ALIST)} and \texttt{(EQUAL X (CAR (CAR ALIST)))} in the \texttt{assoc} definition. Either of these cases will cause the function to halt. The proofs of the base cases are trivial.

The induction step corresponds to the last condition in the \texttt{assoc} definition. This condition leads to the recursive call of \texttt{assoc}. Let \( F(cp, n, tail) \) denotes the main conjecture, i.e.,

\begin{verbatim}
(implies (and (natp n)
              (alistp tail))
  (equal (assoc n (resolveLinks1 tail cp))
         (if (assoc n tail)
             (list n (getConstant n cp))
             nil))))
\end{verbatim}

The induction step can be written as

\begin{verbatim}
(implies (and (not (endp tail))
             (not (eql n (caar tail)))
             (F cp n (cdr tail)))
  (F cp n tail))
\end{verbatim}

ACL2 proves this by simplification appealing to the definitions. With this lemma, ACL2 is able to prove the theorem \texttt{getConstantResolveLinks}.

At this point, we have proved the correctness of the semantic function \texttt{resolveLinks}. The next step is to use \texttt{resolveLinks} to prove that the semantic of \( CP \) is preserved after applying the function \( STF_{form1} \) to it. Our main conjecture is as follows:
(defthm resolveLinks-using-trnsf-is-resolveLinks
  (implies
   (and (natp n)
        (alistp cp))
   (equal (getConstant n (fixStrategy cp))
          (getConstant n (resolveLinks cp))))

This theorem claims if fixStrategy and resolveLinks are given the same constant pool table, then the results of following the resolution chains for an index in both tables are identical. While this result may seem trivial, it provides significant insight into how this approach can be used to verify significant applications written in TL.

6 Related Work

In this section we discuss related work in the areas of rewriting стратегического программирования as well as the verification style we are pursuing.

6.1 Rewriting and Strategic Programming

There are a number of rewriting and strategic systems where a rewrite-based implementation of the class loader core could be considered. Among these systems are ELAN [2], Stratego [22], and ASF+SDF [1]. One of the unique features of TL is its use of higher-order strategies as the mechanism to aggregate data (e.g., all indexes in a constant pool and the Utf8 data to which they resolve) and first-order strategy application as the mechanism to distribute data (e.g., index resolution) throughout a term structure. In contrast, both ELAN and ASF+SDF [5], use parameterization to collect and distribute data throughout a term structure. That is, parameters are added to rewrite rules which can then be passed down and applied at various points within a term structure. In a parameter-based approach, aggregations of data (e.g., all indexes in the constant pool) are typically converted into an internal representation such as a list and must be accompanied with an associated lookup function.

In contrast to parameterization, Stratego supports an approach that arguably can be considered the first-order cousin of higher-order strategy construction mechanisms of TL. Stratego is a first-order strategic programming system that has two constructs related to the higher-order strategies presented in the paper: contextual rules and scoped dynamic rewrite rules. In [21], contextual rules are used to distribute data within a term structure and can be seen as a first-order cousin of the higher-order rules presented in this paper.

In [20], an approach to the distributed data problem is taken that is similar to what we have described. Here the distributed data problem is viewed from a context-free/context-sensitive perspective. In particular, semantic relationships between portions of a term are seen as representing context-sensitive relationships. Dynamic rewrite rules are developed as a mechanism for capturing context-sensitive relationships between portions of a term. Dynamic rewrite rules are named rewrite rules that can be instantiated at runtime (i.e., dynamically) yielding a rule instance which is then added to the existing rule base. Similar to the higher-order approach taken by TL, in Stratego the program itself is the driver
behind the instantiation of dynamic rule variables. The lifetime of dynamic rules can be explicitly constrained in strategy definitions by the scoping operator \{ | \ldots | \}.

Primary differences between our approach and the scoped dynamic rules described in [20] are the following:

1. In our approach, we view the rule base as a strategy that is created dynamically. The $\oplus$ combinator provides the user explicit control over the structure of this strategy.

2. Though the transient combinator has no direct analogy within scoped dynamic rewrite rules, its effects can be simulated in Stratego [23]. However, it is somewhat unclear whether a single approach/method can be used in Stratego to simulate all the behaviors resulting from the interaction between higher-order strategies and transients.

3. The hide combinator has no analogy in Stratego.

6.2 Verification

State transition approach was investigated in [12] [17] [13] [14] In [4], Boyer and Yu used Nqthm [3], the predecessor of ACL2, to formalize a substantial subset of a commercial microprocessor, the Motorola MC68020 [M85]. Based on this model, they were able to verify many binary machine code programs produced by commercial compilers from source code in such high-level languages as Ada, Lisp, and C. In [14], Moore also used the same approach to model Piton, an assembly programming language that is implemented on a microprocessor, the FM8502, via a compiler, an assembler, and a linker. A piton interpreter was coded in the ACL2 logic in which given an initial state $p_0$ you obtain state $p_n$ by running piton forward $n$ steps. However, the alternative approach is to map $p_0$ down to a FM8502 state (or core image), through a function defined in ACL2, run the FM8502, and map the resulting state back up. The compiler, assembler and linker were also defined as functions in the ACL2 logic. The implementation of Piton was mechanically proved correct. In [12] [17][13] ACL2 has been used in verifying the JVM by analyzing the bytecode produced for it. The general approach was to model a significant subset of the JVM operationally using ACL2. This model was used to execute certain Java programs by compiling them into bytecode. The model consists of a state of the JVM and state transition function for each JVM bytecode instruction in the subset. Basically, the state is a triple containing a thread table, a heap, and a class table. The transition function takes an instruction, a thread, and a state, and returns a new state that is the result of executing the given instruction on the given thread in the given state. The new state is a modification of the previous state.

7 Conclusion

From a conceptual standpoint, we believe that transformation provides a natural framework in which the functionality of the class loader core can be considered. However, the intricacy of data interactions as well as the structural complexity of Java class files presents a number of challenges to traditional rewriting and strategic frameworks. Foremost among these challenges is the treatment of term-specific data and its distribution throughout a term structure. Though table construction and parameterization
are techniques capable of realizing data distribution, their use departs from rewriting in its purest sense. Our research is based on the premise that higher-order rewriting provides a mechanism for dealing with the treatment and distribution of term-specific data conforming to the tenets of rewriting. In a higher-order framework, the use of such data is expressed as a rule. Instantiation of such rules can be done using standard (albeit higher-order) mechanisms controlling rule application (e.g., traversal). Typically, a traversal-driven application of a higher-order rule will result in a number of instantiations. If left unstructured, these instantiations can be collectively seen as constituting a rule base whose creation takes place dynamically. However, such rule bases again encounter difficulties with respect to confluence and termination. In order to address this concern the notion of strategy construction is lifted to the higher-order as well. That is, instantiations result in rule bases that are structured to form strategies. Nevertheless, in many cases, simply lifting first-order control mechanisms to the higher-order does not permit the construction of strategies that are sufficiently refined. This difficulty is alleviated though the introduction of the *transient* and *hide* combinators. The interplay between these combinators, higher-order rules, and more traditional control mechanisms enables a the functionality of the class loader core to be concisely expressed. In spite of this, reasoning about the correctness of higher-order strategies is conceptually somewhat of a departure from the reasoning used when considering first-order rewrite rules. Our current efforts in using ACL2 reflects our initial efforts in formalizing our reasoning process in an automatable fashion. This effort involves mapping our approach to reasoning about TL strategies onto proven approaches to reasoning about software.

References


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